

Pre-Calculus Prerequisite Skills

Multiple Choice

Identify the choice that best completes the statement or answers the question.

Use set notation to denote the elements, subsets, and complements of the following given sets.

_____ 1. N is the set of odd natural numbers greater than 11 and less than 21. Use set notation to write the elements of N .

a. $N = \{13, 15, 17, 19\}$

c. $N = \{11, 12, 14, 16, 18, 20, 21\}$

b. $N = \{12, 14, 16, 18, 20\}$

d. $N = \{11, 13, 15, 17, 19, 21\}$

_____ 2. Let $U = \{7, 8, 9, 10, 11, 12\}$ and $A = \{9, 11\}$. Determine whether the statement $A \subset U$ is true or false and find A' .

a. false; $A' = \{9, 10, 11, 12\}$

c. true; $A' = \{7, 8, 9, 10, 12\}$

b. true; $A' = \{7, 8, 10, 12\}$

d. false; $A' = \{7, 10, 12\}$

Find intersections and unions of the following given sets.

3. Let $U = \{2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18\}$, $A = \overset{\ddot{}}{\underset{\circ}{\circ}}6, 12, 13, 15, 16\overset{\acute{}}{\underset{\circ}{\circ}}$, and

$B = \overset{\ddot{}}{\underset{\circ}{\circ}}7, 11, 13, 16\overset{\acute{}}{\underset{\circ}{\circ}}$. Find $A \cup B$ and $A \cap B$.

a. $A \cup B = \overset{\ddot{}}{\underset{\circ}{\circ}}6, 12, 13, 15, 16\overset{\acute{}}{\underset{\circ}{\circ}};$

$A \cap B = \overset{\ddot{}}{\underset{\circ}{\circ}}13, 16\overset{\acute{}}{\underset{\circ}{\circ}}$

c. $A \cup B = \overset{\ddot{}}{\underset{\circ}{\circ}}6, 11, 12, 13, 15, 16\overset{\acute{}}{\underset{\circ}{\circ}};$

$A \cap B = \overset{\ddot{}}{\underset{\circ}{\circ}}11, 15, 16\overset{\acute{}}{\underset{\circ}{\circ}}$

b. $A \cup B = \overset{\ddot{}}{\underset{\circ}{\circ}}6, 7, 11, 12, 13, 15, 16\overset{\acute{}}{\underset{\circ}{\circ}};$

$A \cap B = \overset{\ddot{}}{\underset{\circ}{\circ}}13, 16\overset{\acute{}}{\underset{\circ}{\circ}}$

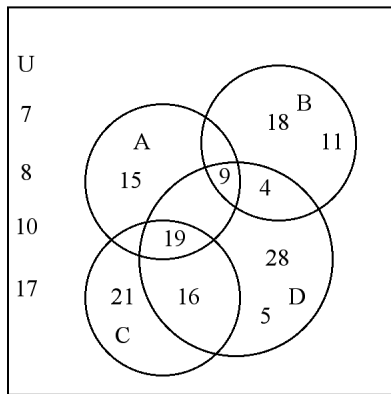
d. $A \cup B = \overset{\ddot{}}{\underset{\circ}{\circ}}6, 7, 11, 12, 13, 15, 16\overset{\acute{}}{\underset{\circ}{\circ}};$

$A \cap B = \overset{\ddot{}}{\underset{\circ}{\circ}}11, 15, 16\overset{\acute{}}{\underset{\circ}{\circ}}$

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_____ 4. Use the Venn diagram to find $A \cup B$, $C \cap D$, and $(A \cup C) \cup D$.



a. $A \cup B = \{4, 9, 11, 15, 18, 19\};$

$C \cap D = \{9, 11, 18, 19, 21, 28\};$

$(A \cup C) \cup D = \{4, 5, 9, 15, 16, 19, 21, 28\}$

b. $A \cup B = \{4, 5, 15, 18, 19\};$

$C \cap D = \{16, 19\};$

$(A \cup C) \cup D = \{4, 5, 11, 13, 15, 18, 19, 21\}$

c. $A \cup B = \{4, 5, 15, 18, 19\};$

$C \cap D = \{9, 11, 18, 19, 21, 28\};$

$(A \cup C) \cup D = \{4, 5, 11, 13, 15, 18, 19, 21\}$

$$d. A \cup B = \{4, 9, 11, 15, 18, 19\};$$

$$C \cap D = \{16, 19\};$$

$$(A \cup C) \cup D = \{4, 5, 9, 15, 16, 19, 21, 28\}$$

_____ 5. Simplify the expression $(3 - 5i)^3$ by performing operations with pure imaginary numbers and complex numbers.

a. $-123 + 10i$

b. $-198 - 10i$

c. $-123 + 550i$

d. $-198 + 550i$

_____ 6. i^7

a. $-i$

b. 1

c. i

d. -1

_____ 7. $(11 + i) + (3 - 15i)$

a. $14 - 14i$

b. $-4 + 4i$

c. $12 - 12i$

d. $14 + 16i$

_____ 8. $(11 - 12i) + (21 - 8i)$

a. $9 + 19i$

b. $32 - 20i$

c. $32 - 4i$

d. $29i - i$

_____ 9. $(8 + 10i)(5 - 8i)$

a. $40 - 14i + 80$

b. $120 - 14i$

c. $40 - 14i - 80i^2$

d. $88 + 50i$

_____ 10. $(-4 + 4i)(-3 - 3i)$

a. $16 + 12i$

b. $12 + 0i - 12i^2$

c. $24 + 0i$

d. $12 + 0i + 12$

_____ 11. Simplify the expression $\frac{3 - 9i\sqrt{5}}{3 + 2i\sqrt{5}}$ by using complex conjugates to write quotients of complex numbers in standard form.

a. $-\frac{9}{19} + \frac{33}{29}i\sqrt{5}$

b. $-\frac{81}{29} - \frac{33}{29}i\sqrt{5}$

c. $-\frac{9}{19} + \frac{60}{19}i\sqrt{5}$

d. $-\frac{81}{29} - \frac{60}{19}i\sqrt{5}$

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_____ 12. Simplify the expression $(4 + 4i) \div (4 - 3i)$ by using complex conjugates to write quotients of complex numbers in standard form.

a. $\frac{4}{19} - \frac{28}{25}i$

c. $\frac{4}{19} + \frac{28}{19}i$

b. $\frac{4}{25} + \frac{28}{25}i$

d. $\frac{4}{25} - \frac{28}{19}i$

_____ 13. $\frac{3}{6 + 7i}$

a. $\frac{18}{85} + \frac{21}{85}i$

c. $\frac{18}{13} + \frac{21}{13}i$

b. $\frac{6}{85} - \frac{7}{85}i$

d. $\frac{18}{85} - \frac{21}{85}i$

_____ 14. $\frac{6 - 3i}{8 - 11i}$

a. $\frac{81}{185} + \frac{42}{185}i$

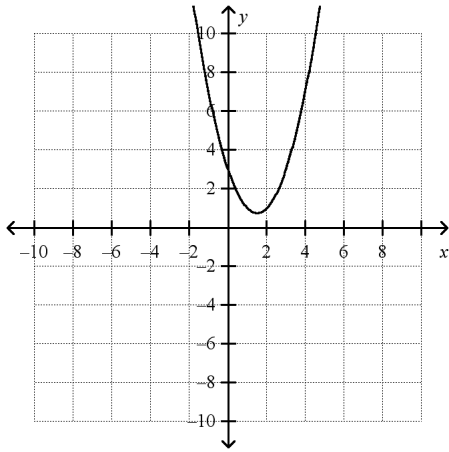
c. $\frac{6}{185} - \frac{3}{185}i$

b. $\frac{15}{57} + \frac{42}{57}i$

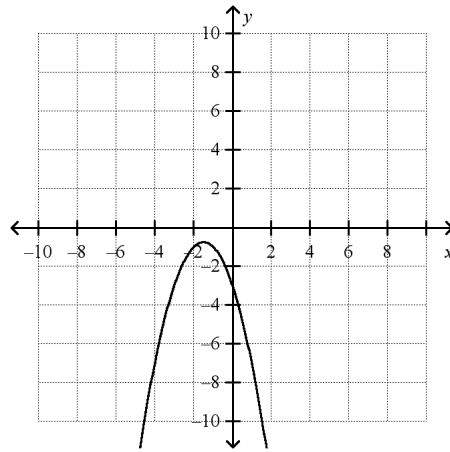
d. $\frac{81}{185} - \frac{42}{185}i$

_____ 15. Graph $f(x) = x^2 + 3x + 3$ by making a table of values.

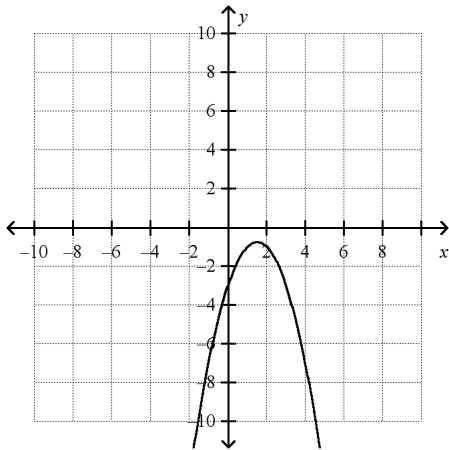
a.



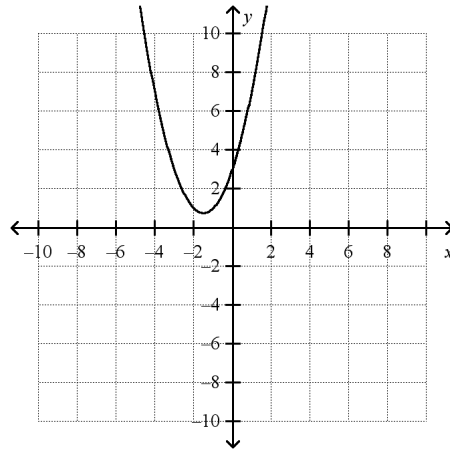
c.



b.



d.



_____ 16. Consider $f(x) = 2x^2 + 8x + 3$. Determine whether the function has a maximum or minimum value. Then find the value of the maximum or minimum.

- a. maximum; -2
- b. minimum; -5
- c. minimum; -2
- d. maximum; -5

_____ 17. Solve the equation $x^2 - 9x + 20 = 0$.

- a. 4, -5
- b. 4, 5
- c. -4, 5
- d. -4, 5

_____ 18. Solve $x^2 + 2x = 15$ by completing the square.

- a. 3, -5
- b. 6, -2
- c. 5, -15
- d. 4, -15

- _____ 19. Solve $x^2 - 4x - 32 = 0$ by completing the square.
 a. $-4, 8$ c. $-8, 4$
 b. $-8, 16$ d. $-8, 8$
- _____ 20. Solve $-2x^2 + 5x = 0$ by completing the square.
 a. $2.5, 0$ c. 0
 b. $0, -2.5$ d. $5, 0$
- _____ 21. Find the exact solution of $x^2 - 3x = 40$ by using the Quadratic Formula.
 a. $-5, 8$ c. $-10, 16$
 b. $-8, 5$ d. $40, 43$
- _____ 22. Find the exact solution of $-x^2 + 3x + 7 = 0$ by using the Quadratic Formula.
 a. $\frac{3 - \sqrt{37}}{-2}, \frac{3 + \sqrt{37}}{-2}$ c. $\frac{-3 - \sqrt{-19}}{-2}, \frac{-3 + \sqrt{-19}}{-2}$
 b. $\frac{-3 - \sqrt{12}}{-2}, \frac{-3 + \sqrt{12}}{-2}$ d. $\frac{-3 - \sqrt{37}}{-2}, \frac{-3 + \sqrt{37}}{-2}$
- _____ 23. Simplify the expression: $\sqrt{16a^{10}}$
 a. $16a^{10}$ c. $4a^{10}$
 b. $16a^5$ d. $4a^5$
- _____ 24. Simplify $\sqrt{25x^{20}y^{14}}$.
 a. $5x^{10}y^7$ c. $5x^{20}y^{14}$
 b. $12.5x^{20}y^{14}$ d. $12.5x^{10}y^7$
- _____ 25. Simplify $\sqrt[4]{81a^{32}b^{20}}$.
 a. $20.25a^{32}b^{20}$ c. $3a^8b^5$
 b. $3a^{32}b^{20}$ d. $20.25a^8b^5$
- _____ 26. Simplify $\sqrt{72x^5y^{12}}$.
 a. $6y^6\sqrt{2x^5}$ c. $6x^2y^6\sqrt{x}$
 b. $6\sqrt{2x^5y^{12}}$ d. $6x^2y^6\sqrt{2x}$
- _____ 27. Simplify $\sqrt{1331x^{13}y^{12}}$.
 a. $11y^6\sqrt{11x^{13}}$ c. $11\sqrt{11x^{13}y^{12}}$
 b. $11x^6y^6\sqrt{x}$ d. $11x^6y^6\sqrt{11x}$

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_____ 28. Simplify the expression. $\frac{x^{\frac{4}{7}} \cdot x^{\frac{3}{7}}}{x^{\frac{1}{7}}}$

a. $x^{\frac{7}{8}}$

c. $x^{\frac{7}{6}}$

b. $x^{\frac{6}{7}}$

d. $x^{\frac{8}{7}}$

_____ 29. Solve the following system of equations. State whether the system is *consistent and independent*, *consistent and dependent*, or *inconsistent*.

$$-5x + 3y = 15$$

$$5x - 3y = 20$$

a. *inconsistent*

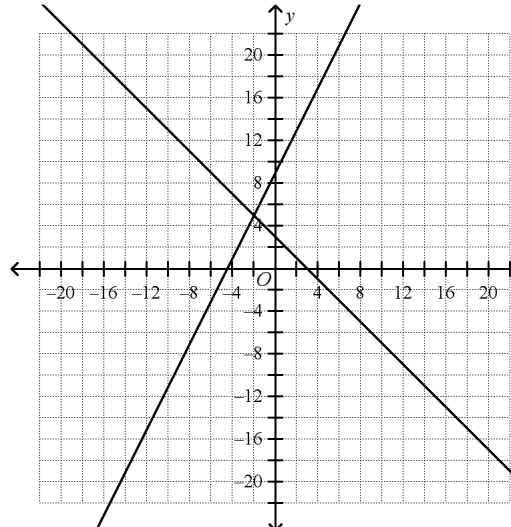
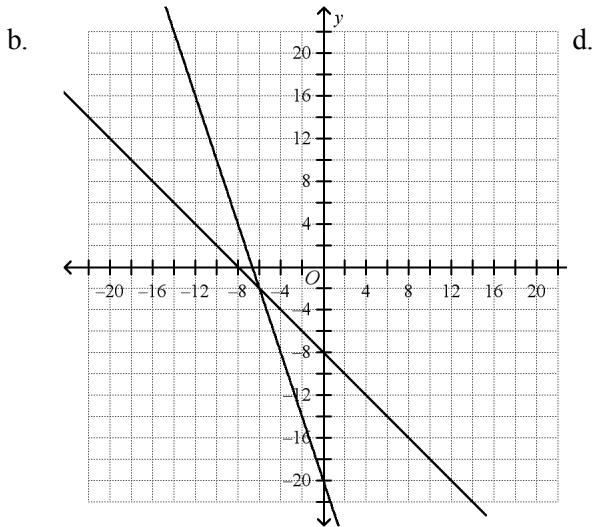
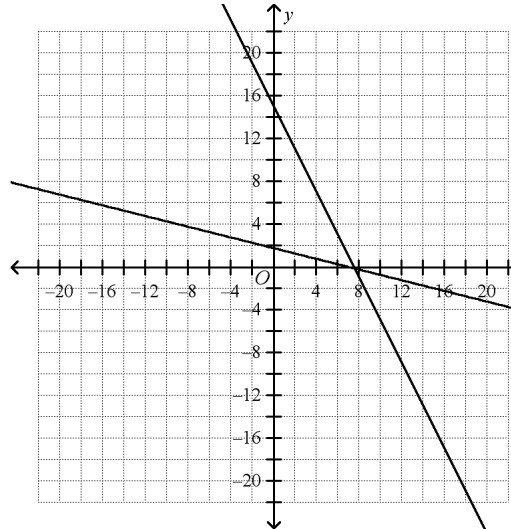
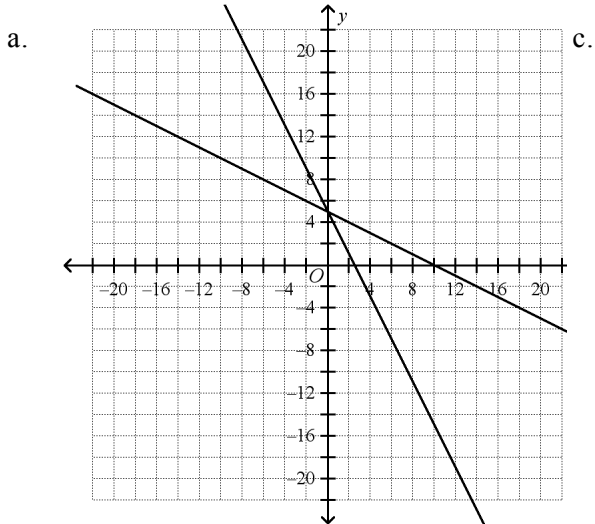
b. *consistent and dependent*

c. *consistent and independent*

____ 30. Solve the system of equations by graphing.

$$x + y = -8$$

$$3x + y = -20$$



_____ 31. Solve the system of equations algebraically.

$$4x - 3y = 3$$

$$6x - 6y = 6$$

a. many solutions

b. $\begin{matrix} \hat{E} \\ \uparrow \\ \hat{A} \\ \uparrow \\ \hat{E} \end{matrix} -1, 0$

c. $\begin{matrix} \hat{E} \\ \uparrow \\ \hat{A} \\ \uparrow \\ \hat{E} \end{matrix} 0, -1$

d. no solution

_____ 32. Solve the system of equations.

$$2x + 4y + 3z = 6$$

$$3x + 5y + 6z = 3$$

$$2x + 3y + 4z = 8$$

a. $\begin{matrix} \hat{E} \\ \uparrow \\ \hat{A} \\ \uparrow \\ \hat{E} \end{matrix} x = 63, y = -18, z = -16$

b. $\begin{matrix} \hat{E} \\ \uparrow \\ \hat{A} \\ \uparrow \\ \hat{E} \end{matrix} x = 65, y = -20, z = -14$

c. $\begin{matrix} \hat{E} \\ \uparrow \\ \hat{A} \\ \uparrow \\ \hat{E} \end{matrix} x = 62, y = -17, z = -15$

d. $\begin{matrix} \hat{E} \\ \uparrow \\ \hat{A} \\ \uparrow \\ \hat{E} \end{matrix} x = 64, y = -19, z = -17$

_____ 33. Solve the system of equations by graphing.

$$y = 11x - 6$$

$$y = -6x + 11$$

a. $(-1, 5)$

b. $(1, 7)$

c. $(5, 1)$

d. $(1, 5)$

_____ 34. Solve the system of equations by graphing.

$$2y + 8x = 58$$

$$y - 5x = 11$$

a. $(2, 21)$

b. $(21, 2)$

c. $(4, 20)$

d. $(1, 21)$

_____ 35. State whether the system of equations is *consistent and independent*, *inconsistent*, *consistent and dependent*, or *none of these*.

$$5x - 8y = 6$$

$$6x - 6y = 6$$

a. inconsistent

b. consistent and independent

c. consistent and dependent

d. none of these

_____ 36. Solve the system of equations by using substitution.

$$8x + 7y = 18$$

$$3x - 5y = 22$$

a. $(-2, 4)$

b. $(3, -2)$

c. $(4, -2)$

d. $(4, 0)$

_____ 37. Solve the system of equations by using substitution.

$$3r + 3s = 9$$

$$3r - 6s = 18$$

a. $(4, -0.5)$

b. $(5.5, 3)$

c. $(4, -1)$

d. $(2, -1)$

_____ 38. Solve the system of equations by using elimination.

$$3p + 9q = 6$$

$$5p - 5q = 30$$

a. $(6, -1)$

b. $(3.75, 2)$

c. $(5, 0.5)$

d. $(5, -1)$

_____ 39. Solve the system of equations by using elimination.

$$7a + 9b = 14$$

$$6a - 4b = 12$$

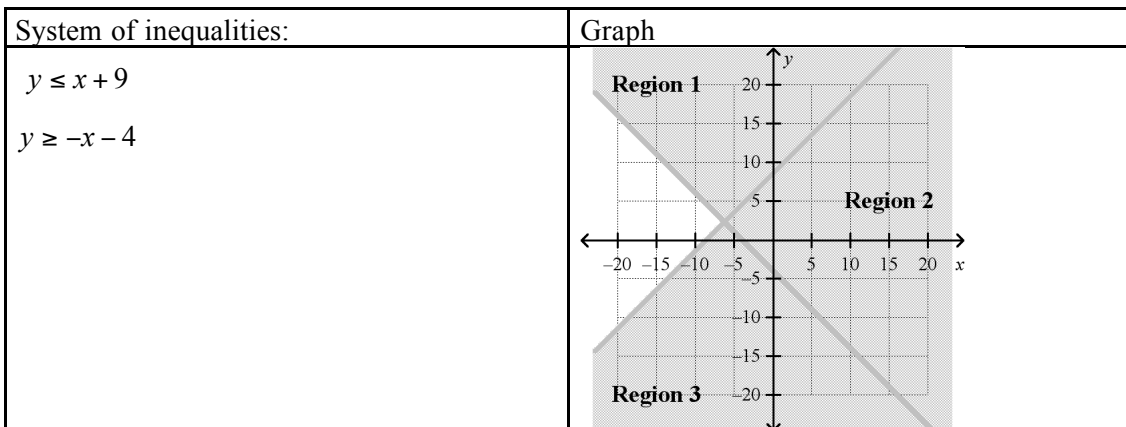
a. $(2, 0.25)$

b. $(2, 0)$

c. $(1, 0)$

d. $(3, -0.5)$

_____ 40. Which region in the graph below is the solution of the system of inequalities given below?



a. Region 3

b. Region 2

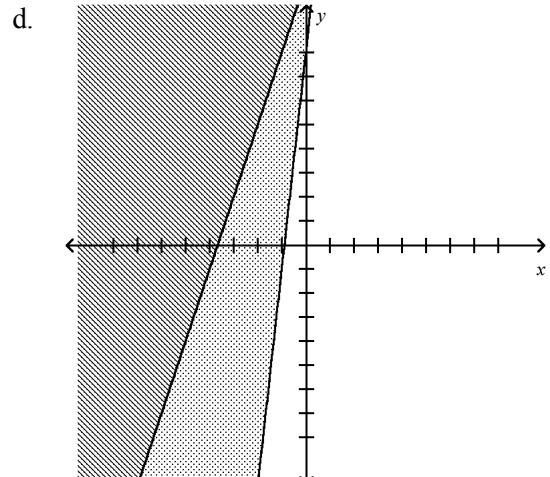
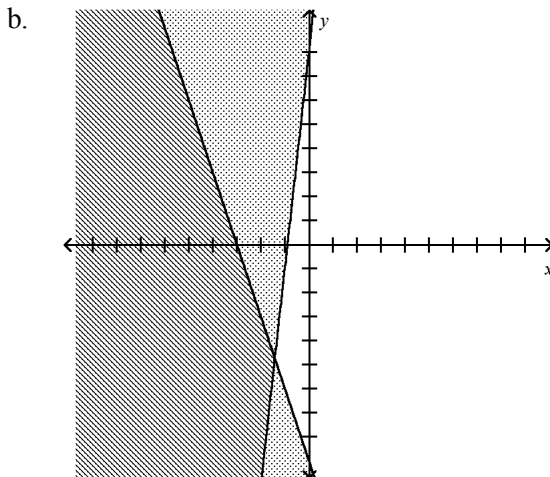
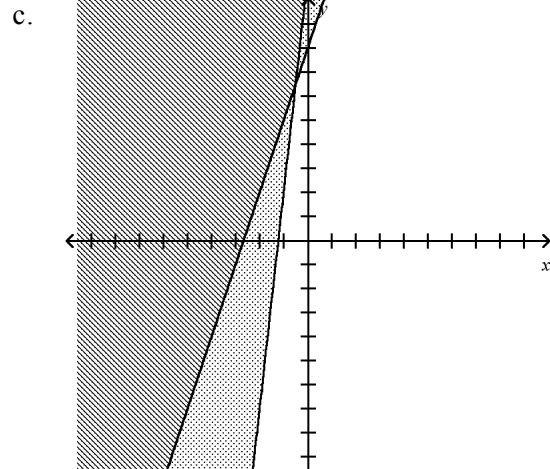
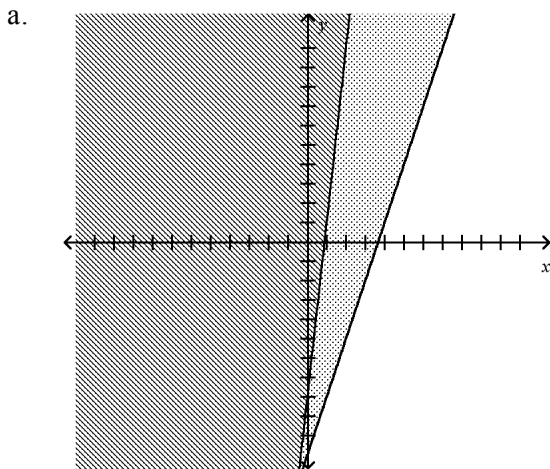
c. Region 1

d. Regions 1 and 2

____ 41. Solve the system of inequalities by graphing.

$$y \leq -3x + 9$$

$$y \geq 9x + 8$$



Use characteristics to describe the following matrix.

____ 42. Use $A = \begin{bmatrix} \vec{E} & & & \\ 10 & 4 & 11 & 12 \\ 6 & 3 & 2 & 8 \end{bmatrix}$ to find the value of A_{21} .

- a. 6
- b. 10

- c. 3
- d. 4

Perform the following operations for the given matrices.

_____ 43. Find each of the following for $A = \begin{bmatrix} \tilde{E} & & \\ 7 & 5 & 4 \\ 2 & 8 & 12 \end{bmatrix}$ and $B = \begin{bmatrix} \tilde{E} & & \\ 11 & 2 & 9 \\ 12 & 8 & 4 \end{bmatrix}$.

a. $A + B$

b. $5A - B$

a. $A + B = \begin{bmatrix} \tilde{E} & & \\ 18 & 7 & 13 \\ 14 & 16 & 16 \end{bmatrix};$

$5A - B = \begin{bmatrix} \tilde{E} & & \\ 24 & 23 & 11 \\ -2 & 32 & 56 \end{bmatrix}$

c. $A + C = \begin{bmatrix} \tilde{E} & & \\ 18 & 7 & 13 \\ 14 & 8 & 16 \end{bmatrix};$

$5A - B = \begin{bmatrix} \tilde{E} & & \\ 24 & 23 & 11 \\ 58 & 32 & 56 \end{bmatrix}$

b. $A + B = \begin{bmatrix} \tilde{E} & & \\ 21 & 7 & 17 \\ 14 & 8 & 16 \end{bmatrix};$

$5A - B = \begin{bmatrix} \tilde{E} & & \\ 48 & 5 & 41 \\ 58 & 32 & 8 \end{bmatrix}$

d. $A + C = \begin{bmatrix} \tilde{E} & & \\ 21 & 7 & 17 \\ 14 & 8 & 16 \end{bmatrix};$

$5A - B = \begin{bmatrix} \tilde{E} & & \\ 48 & 23 & 41 \\ 58 & 32 & 8 \end{bmatrix}$

_____ 44. If $A = \begin{bmatrix} \tilde{E} & & \\ 3 & 8 & -2 \\ -1 & 5 & 2 \\ 9 & -3 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} \tilde{E} & & \\ 9 & 2 & 6 \\ 2 & 5 & 5 \\ 3 & 5 & 2 \end{bmatrix}$, find $A + B$.

a. $\begin{bmatrix} \tilde{E} & & \\ 14 & 9 & 6 \\ -1 & 11 & 9 \\ 11 & -2 & 5 \end{bmatrix}$

b. $\begin{bmatrix} \tilde{E} & & \\ 12 & 10 & 4 \\ 1 & 10 & 7 \\ 12 & 2 & 6 \end{bmatrix}$

c. $\begin{bmatrix} \tilde{E} & & \\ 11 & 12 & 5 \\ 7 & 9 & 6 \\ 14 & 0 & 4 \end{bmatrix}$

d. $\begin{bmatrix} \tilde{E} & & \\ 12 & 8 & 2 \\ 0 & 8 & 6 \\ 15 & 9 & 2 \end{bmatrix}$

_____ 45. Find $\begin{bmatrix} \vec{E} & 6 \\ -4 \\ 5 \end{bmatrix} + \begin{bmatrix} \vec{E} & -5 \\ -9 \\ 9 \end{bmatrix}$.

a. $\begin{bmatrix} \vec{E} & -1 \\ 13 \\ 14 \end{bmatrix}$

b. $\begin{bmatrix} \vec{E} & -11 \\ -5 \\ 14 \end{bmatrix}$

c. $\begin{bmatrix} \vec{E} & 1 \\ -13 \\ 14 \end{bmatrix}$

d. $\begin{bmatrix} \vec{E} & 11 \\ 5 \\ 14 \end{bmatrix}$

_____ 46. $\begin{bmatrix} \vec{E} & 4 & 5 \\ -3 & -6 \end{bmatrix} + \frac{1}{2} \begin{bmatrix} \vec{E} & 0 & 6 \\ -6 & -4 \end{bmatrix}$

a. $\begin{bmatrix} \vec{E} & 2 & 5.5 \\ -4.5 & -5 \end{bmatrix}$

b. $\begin{bmatrix} \vec{E} & 4 & 8 \\ -9 & -10 \end{bmatrix}$

c. $\begin{bmatrix} \vec{E} & 4 & 8 \\ -6 & -8 \end{bmatrix}$

d. $\begin{bmatrix} \vec{E} & 2 & 8.5 \\ -7.5 & -7 \end{bmatrix}$

_____ 47. $\begin{bmatrix} \vec{E} & 5 & 9 \\ -3 & -9 \end{bmatrix} - \begin{bmatrix} \vec{E} & 0 & 2 \\ -2 & -6 \end{bmatrix}$

a. $\begin{bmatrix} \vec{E} & 5 & 7 \\ 3 & -7 \end{bmatrix}$

b. $\begin{bmatrix} \vec{E} & 5 & 7 \\ -1 & -3 \end{bmatrix}$

c. $\begin{bmatrix} \vec{E} & 3 & 9 \\ 3 & -7 \end{bmatrix}$

d. $\begin{bmatrix} \vec{E} & -5 & -7 \\ 1 & 3 \end{bmatrix}$

_____ 48. $3 \begin{bmatrix} \tilde{E} & & \\ 4 & 2 & \\ -2 & -8 & \end{bmatrix} - 2 \begin{bmatrix} \tilde{E} & & \\ 0 & 6 & \\ -8 & -2 & \end{bmatrix}$

a. $\begin{bmatrix} \tilde{E} & & \\ 12 & -6 & \\ -2 & -8 & \end{bmatrix}$

c. $\begin{bmatrix} \tilde{E} & & \\ 0 & 6 & \\ -2 & -8 & \end{bmatrix}$

b. $\begin{bmatrix} \tilde{E} & & \\ 12 & -6 & \\ 10 & -20 & \end{bmatrix}$

d. $\begin{bmatrix} \tilde{E} & & \\ -4 & 4 & \\ -6 & 6 & \end{bmatrix}$

_____ 49. If $A = \begin{bmatrix} \tilde{E} & & \\ -3 & 7 & -5 \\ 3 & 7 & 9 \end{bmatrix}$, find $-4A$.

a. $\begin{bmatrix} \tilde{E} & & \\ 12 & -28 & 20 \\ -12 & -28 & -36 \end{bmatrix}$

c. $\begin{bmatrix} \tilde{E} & & \\ -12 & -28 & -20 \\ -12 & -28 & -36 \end{bmatrix}$

b. $\begin{bmatrix} \tilde{E} & & \\ 12 & -28 & 20 \\ 3 & 7 & 9 \end{bmatrix}$

d. $\begin{bmatrix} \tilde{E} & & \\ -12 & 28 & -20 \\ 12 & 28 & 36 \end{bmatrix}$

_____ 50. Use $A = \begin{bmatrix} \tilde{E} & & \\ 1 & 5 & \\ -3 & 6 & \end{bmatrix}$, $B = \begin{bmatrix} \tilde{E} & & \\ 3 & 9 & \\ 1 & -1 & \end{bmatrix}$, and $C = \begin{bmatrix} \tilde{E} & & \\ 4 & 6 & \\ -2 & -8 & \end{bmatrix}$ to determine whether

$A(B+C) = AB+AC$ for the given matrices.

a. Yes

b. No

_____ 51. A bookstore offers a collection of books. A student can select from one of 6 algebra books, one of 4 geometry books, and one of 3 calculus books. How many different possibilities are available for that collection?

a. 48

c. 36

b. 30

d. 72

_____ 52. How many ways can 6 different books be stacked on a shelf?

a. 720

c. 24

b. 120

d. 6

_____ 53. Find the value of ${}_6P_4$.

a. 15

c. 24

b. 2

d. 360

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_____ 54. How many ways can the top 5 teams be arranged in a league containing 21 teams?

- a. 15,504
- b. 143,640
- c. 2,441,880
- d. 1,860,480

_____ 55. In a race between 21 people, how many ways can the top 6 finishers be arranged?

- a. 39,070,080
- b. 54,264
- c. 27,907,200
- d. 2,441,880

_____ 56. How many committees of 3 people can be chosen from a group of 12 people?

- a. 1,320
- b. 220
- c. 165
- d. 66

_____ 57. From a class of 24 students, how many ways can a group of 7 students be chosen?

- a. 245,157
- b. 134,596
- c. 1,744,364,160
- d. 346,104

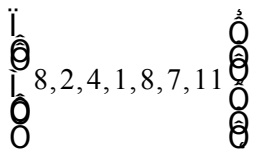
_____ 58. Find $P(5, 3)$.

- a. 20
- b. 60
- c. 10
- d. 15

_____ 59. Find $C(9, 5)$.

- a. 45
- b. 126
- c. 15,120
- d. 84

_____ 60. Find the mean for the data set



- a. 5.86
- b. 5.50
- c. 8
- d. 7

_____ 61. Find the standard deviation for the given data.

5, 6, 8, 11, 10

- a. 3.28
- b. 1.28
- c. 2.28
- d. 4.28

_____ 62. Find the variance and standard deviation of the given set of data to the nearest tenth.

{450, 180, 380, 400, 160, 570, 780}

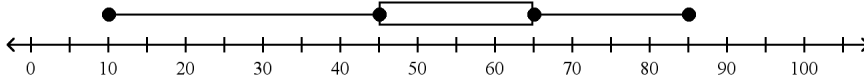
- a. variance = 40,020.4, standard deviation = 200.1
- b. variance = 46,690.5, standard deviation = 216.1
- c. variance = 200.1, standard deviation = 40,020.4
- d. variance = 40,020.4, standard deviation = 20,010.2

_____ 63. Find the variance and standard deviation for the given set of data to the nearest tenth.

{5.1, 14.5, 22.7, 34.3, 22, 41.8, 18.3, 46, 15, 61.8}

- a. variance = 16.5, standard deviation = 273
- b. variance = 303.4, standard deviation = 17.4
- c. variance = 273, standard deviation = 16.5
- d. variance = 273, standard deviation = 136.5

Jeffery surveyed 50 randomly selected workers at a factory. He collected data about the individual output of a worker on an average day. The results are shown using the box-and-whisker plot.



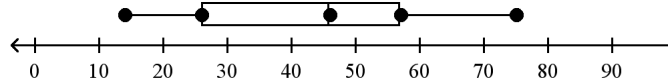
_____ 64. What percent of workers have output more than 65 units?

- a. 35%
- b. 50%
- c. 25%
- d. 18%

_____ 65. What is the interquartile range of the box-and-whisker plot shown?

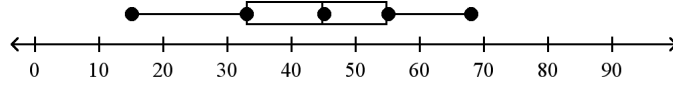
- a. 15
- b. 5
- c. 20
- d. 65

_____ 66. Find the range of the data shown on the box-and-whisker plot below.



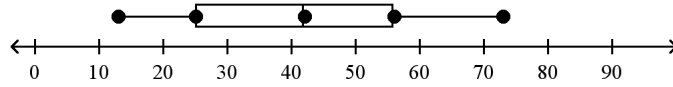
- a. 46
- b. 49
- c. 61
- d. 31

_____ 67. Find the median of the data shown on the box-and-whisker plot below.



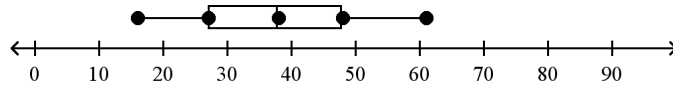
- a. 45
- b. 35
- c. 53
- d. 22

_____ 68. Find the upper quartile of the data shown on the box-and-whisker plot below.



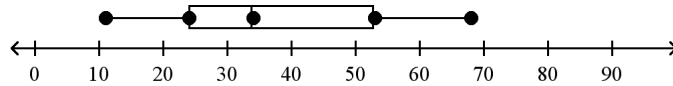
- a. 42
- b. 73
- c. 56
- d. 31

_____ 69. Find the lower quartile of the data shown on the box-and-whisker plot below.



- a. 38
- b. 16
- c. 27
- d. 21

_____ 70. Find the interquartile range of the data shown on the box-and-whisker plot below.



- a. 53
- b. 57
- c. 24
- d. 29

Short Answer

Let $U = \{-5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5\}$, $M = \{-4, -2, 0\}$, $N = \{-4, -3, -2, 3, 5\}$, $P = \{-5, -1, 2, 4, 5\}$, and $Q = \{2, 5\}$.

71. State whether $M \in N$ is *true* or *false*.
72. State whether $Q \in P$ is *true* or *false*.
73. Find the complement of N .
74. Find the complement of P .
75. Use set notation to write the elements of the following set.

B is the set of negative numbers greater than -7 .

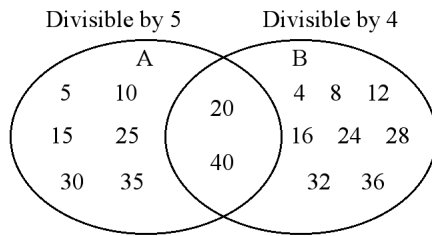
Find intersections and unions of the following given sets.

76. Let $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\}$, $A = \{1, 3, 5\}$, and $B = \{2, 4, 6, 8\}$. Find $A \cup B$ and $A \cap B$.
77. Let $U = \{21, 22, 23, 24, 31, 32, 33, 34, 41, 42, 43, 44\}$, $M = \{22, 32, 42, 44\}$, and $N = \{21, 31, 33, 42, 44\}$. Find $M \cup N$ and $M \cap N$.
78. Ten students from a school appear in one or more subjects for an inter school quiz competition as shown in the table given below.

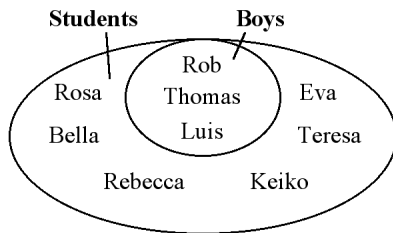
General Knowledge	Math	Science
Acel	Barek	Carlin
Acton	Bay	Acton
Anael	Max	Anael
Max	Kai	Kai
Carl	Anael	Dario
Dario	Carlin	Barek

Let G represents the set of students appearing for General Knowledge, M represents the set of students appearing for Math, and S represents the set of students appearing for Science.
Find $G \cap M$ and $G \cup S$.

79. Use the Venn diagram to identify
- $A \cap B$
- and
- $A \cup B$
- .



80. Use the Venn diagram to identify intersections and unions.



For the following question perform operations with pure imaginary numbers and complex numbers.

81. Simplify the power of
- i
- .

$$i^{531}$$

82. Simplify the expression
- $0.23 - (0.46 - 0.19i) + 0.67i$
- .

83. Simplify the expression
- $(8 - 9i)(2 - 4i) + (5 - 6i)$
- .

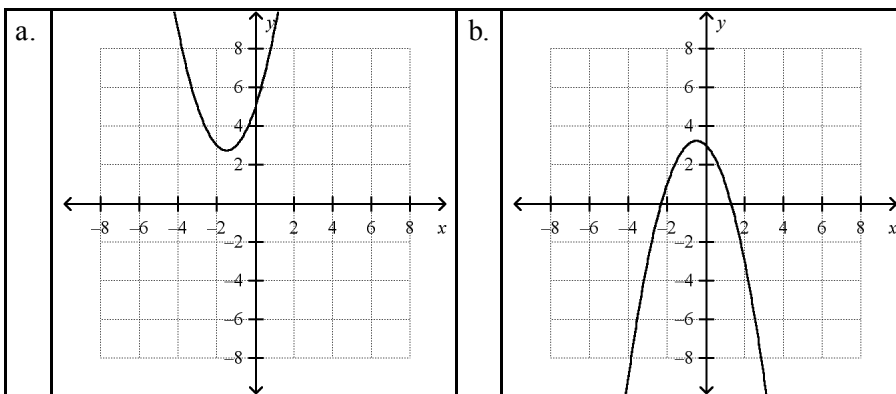
84. In an alternating-current circuit, the voltage
- E
- is given by
- $E = IZ$
- , where
- I
- is the current (in A) and
- Z
- is the impedance (in
- Ω
-). Each of these can be represented by complex numbers. Find the complex number representation for
- E
- if
- $I = 0.835 - 0.427i$
- amperes and
- $Z = 250 + 170i$
- ohms.

Use complex conjugates to write quotients of complex numbers in standard form for the following questions.

85. Simplify the expression
- $\frac{i\sqrt{2} - 5}{i\sqrt{2} + 3}$
- .

86. Simplify the expression
- $\frac{3 - \sqrt{5}i}{2 + \sqrt{3}i}$
- .

87. In an alternating-current circuit, the voltage E is given by $E = IZ$, where I is the current (in A) and Z is the impedance (in Ω). Each of these can be represented by complex numbers. Find the complex number representation for Z if $I = 0.235 - 0.527i$ amperes and $E = 5.20 + 1.70i$ volts.
88. In an alternating-current circuit, the voltage E is given by $E = IZ$, where I is the current (in A) and Z is the impedance (in Ω). Each of these can be represented by complex numbers. Find the complex number representation for I if $E = 22 + 8i$ volts and $Z = 200 - 70i$ ohms.
89. In an alternating-current circuit, the voltage E is given by $E = IZ$, where I is the current (in A) and Z is the impedance (in Ω). Each of these can be represented by complex numbers. Find the complex number representation for I if $E = 62 + 32i$ volts and $Z = 1200 - 560i$ ohms.
90. Graph $f(x) = x^2 - 2x - 5$ by making a table of values.
91. Graph $f(x) = -x^2 - 3x - 4$ by making a table of values.
92. Determine whether each function has a maximum or minimum value.



93. Use the axis of symmetry, y -intercept, and vertex to graph $f(x) = x^2 + 4x - 5$.
94. Consider $f(x) = -2x^2 + 4x + 7$. Determine whether the function has a maximum or minimum value. Then find the value of the maximum or minimum.
95. Solve the equation $x^2 - 6x + 5 = 0$.
96. Solve the equation $x^2 - 4x + 18 = 0$.
97. Solve the equation $x^2 - 10x + 22 = 0$.
98. Solve $3x^2 - 3x - 3 = 0$ by completing the square.

99. Simplify the expression: $\sqrt[6]{x^{30}}$

100. Simplify the expression: $\sqrt[5]{\frac{243}{32}}$

101. Simplify the expression: $-\sqrt{121}$

102. Simplify the expression: $\sqrt[6]{-169}$

103. Simplify the expression: $\frac{\sqrt[8]{81}}{\sqrt[6]{3}}$

104. Simplify the expression: $\sqrt[4]{a^{15}b^9}$

105. Simplify the expression: $\frac{64^{\frac{5}{4}}}{64^{\frac{3}{4}}}$

106. Simplify the expression $\sqrt[3]{3x^3y^{-5}}$.

107. Evaluate $(125)^{\frac{-2}{3}}$.

108. Solve the following system of equations by graphing.

$$2x + 5y = -10$$

$$x + y = -5$$

109. Solve the following system of equations. State whether the system is *consistent and independent*, *consistent and dependent*, or *inconsistent*.

$$2x + 3y = 15$$

$$8x + 12y = 60$$

110. Use substitution method to solve the system of equations.

$$7x - y = 12$$

$$5x + y = 12$$

111. Solve the system of equations by graphing.

$$x + y = 6$$

$$2x - 6y = 4$$

112. Solve the system of equations algebraically.

$$2x + y = 1$$

$$-7x + 5y = 5$$

113. Solve the system of equations.

$$2x + 9y + 9z = 4$$

$$2x + 5y + 2z = 7$$

$$2x + 9y + 7z = 6$$

114. Solve the system of inequalities by graphing.

$$y > 5x + 2$$

$$y < 5x - 7$$

115. Solve the system of inequalities by graphing.

$$y \leq 0.2x + 3$$

$$y \geq -5x + 1$$

116. Solve the system of inequalities by graphing.

$$y \geq 0.5x - 1$$

$$y \leq -2x + 5$$

117. Solve the system of inequalities by graphing.

$$y \leq 7x - 1$$

$$-3x + 3y \geq -4$$

Use $M = \begin{bmatrix} 2 & 3 & 12 & 5 \\ 1 & 7 & 13 & 9 \\ 10 & 4 & 8 & 11 \\ 17 & 18 & 20 & 21 \end{bmatrix}$ to answer the following.

118. State the dimensions of M .

119. Find the value of M_{23} and M_{41} .

Find each of the following for $A = \begin{bmatrix} 4 & 1 & 2 \\ 12 & 7 & 8 \\ 5 & 11 & 10 \end{bmatrix}$, $B = \begin{bmatrix} 2 & 13 & 1 \\ 12 & 8 & 7 \\ 9 & 15 & 10 \end{bmatrix}$, $C = \begin{bmatrix} 1 & 2 \\ 4 & 7 \end{bmatrix}$, and

$$D = \begin{bmatrix} 8 & 9 \\ 4 & 1 \end{bmatrix}.$$

120. Find $A + B$.

121. Find $A - B$.

122. Find $2C + 3D$.

123. Find $A + D$.

124. If $A = \begin{bmatrix} 6 & 4 & 7 \\ 0 & 3 & 4 \\ 9 & 6 & 4 \end{bmatrix}$ and $B = \begin{bmatrix} 9 & 9 & 6 \\ 9 & 9 & 2 \\ 5 & 9 & 1 \end{bmatrix}$, find $A + B$

125. In how many ways can seven different books be arranged on a shelf if the books can be placed in any order?

126. A restaurant offers a lunch special in which a customer can select from one of the 7 appetizers, one of the 10 entrees, and one of the 6 desserts. How many different lunch specials are possible?

Three balls are drawn at random from a bag containing 4 white balls, 3 red balls, and 6 black balls.

127. What is the probability of getting 2 red balls and 1 black ball?
128. What is the probability of getting 3 white balls?

129. Find the mean, median and mode for the data set $\overset{\cdot}{\underset{\cdot}{\text{O}}}$ 330, 360, 300, 400, 360, 360, 300 $\overset{\cdot}{\underset{\cdot}{\text{O}}}$.

130. Seven students participated in a game. Time (in minutes) required to complete the game is listed below. Find the measures of spread.
13, 11, 18, 13, 13, 13, 14

131. Make a box-and-whisker plot for the set of data below.

82, 64, 33, 77, 42, 27, 35, 32, 39, 34

Marks of 25 students listed below.

10, 15, 9, 8, 21, 25, 28, 31, 35, 38, 15, 16, 9, 35, 39, 41, 43, 48, 38, 15, 29, 35, 41, 16, 27

132. Make a frequency distribution for the data. Then determine the relative frequency distribution.
133. Construct a histogram for both the frequency distribution and the relative frequency distribution. Then compare the graphs.
134. Define cumulative frequency and cumulative relative frequency for a class.
135. Make a cumulative frequency distribution for the data. Then determine the cumulative relative frequency distribution.
136. Construct a histogram for the cumulative frequency distribution.